

Quantum Transport in Dirac and Weyl Semimetals: Electronic Properties and Applications

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ABSTRACT

Quantum transport in Dirac and Weyl semimetals has emerged as a pivotal research area in solid-state physics due to its implications for topological materials, electronic transport phenomena, and next-generation quantum devices. Unlike conventional semiconductors and metals, Dirac and Weyl semimetals exhibit massless quasiparticles, chiral anomaly, negative magnetoresistance, and unique topological properties that distinguish them from other electronic materials. These properties arise from their nontrivial band structures, where electronic states are governed by relativistic-like equations analogous to those of high-energy particle physics. This study explores the fundamental principles governing quantum transport in Dirac and Weyl semimetals, emphasizing their topological band structures, carrier dynamics, and magneto transport phenomena. We analyze key quantum effects, such as the Shubnikov–de Haas (SdH) and de Haas–van Alphen (dHvA) oscillations, weak anti-localization, and the anomalous Hall effect, which are critical for understanding charge carrier behavior in these materials. Additionally, we discuss recent experimental advancements in angle-resolved photoemission spectroscopy (ARPES), electrical resistivity measurements, and scanning probe techniques used to characterize these quantum transport properties. Beyond fundamental physics, Dirac and Weyl semimetals hold significant potential for applications in high-mobility transistors, quantum computing, spintronics, and valleytronics. Their low-energy dissipation, high carrier mobility, and robustness against defects make them attractive candidates for future electronic and quantum information processing technologies. However, challenges remain in material synthesis, stability, and integration with existing semiconductor technologies. This paper provides a comprehensive review of quantum transport phenomena in Dirac and Weyl semimetals, covering both theoretical and experimental perspectives. We conclude with an outlook on the future research directions, including the role of machine learning in material discovery and the quest for room-temperature topological superconductors.

Keywords: Quantum transport, Dirac and Weyl semimetals, Electronic properties

1. INTRODUCTION

1.1 Background on Dirac and Weyl Semimetals

The discovery of Dirac and Weyl semimetals has significantly expanded the field of condensed matter physics by introducing new paradigms in quantum transport and topological electronic materials. These materials, unlike conventional semiconductors and metals, exhibit electronic excitations that behave as

massless Dirac or Weyl fermions, similar to those found in high-energy physics. Dirac semimetals (e.g., Cd_3As_2 and Na_3Bi) possess fourfold-degenerate Dirac points where conduction and valence bands touch, while Weyl semimetals (e.g., TaAs and NbP) break either time-reversal or inversion symmetry, leading to twofold-degenerate Weyl nodes. The existence of these nodes gives rise to exotic quantum transport phenomena, such as the chiral anomaly, anomalous Hall effect, and negative magnetoresistance, which are absent in conventional electronic systems.

1.2 Importance of Quantum Transport in Dirac and Weyl Semimetals

Quantum transport refers to the behavior of charge carriers at nanometer scales, where wave-like properties of electrons become prominent due to quantum coherence effects. In Dirac and Weyl semimetals, transport is significantly influenced by their topologically protected band structures, leading to novel physical effects:

- **High Carrier Mobility:** Due to the linear dispersion relation of Dirac and Weyl fermions, charge carriers can propagate with minimal scattering, leading to exceptionally high carrier mobility, making these materials promising for ultra-fast electronics.
- **Negative Magnetoresistance (Chiral Anomaly):** The axial anomaly in Weyl semimetals results in charge pumping between Weyl nodes of opposite chirality, leading to negative longitudinal magnetoresistance—a hallmark feature of these materials.
- **Quantum Oscillations:** Shubnikov–de Haas (SdH) and de Haas–van Alphen (dHvA) oscillations provide key insights into the Fermi surface and Berry phase effects in these materials.
- **Weak Antilocalization and Anomalous Hall Effect:** The nontrivial topology of these materials leads to weak antilocalization, protecting them against Anderson localization, and results in large anomalous Hall conductivities.

These unique transport properties open up new possibilities for applications in quantum computing, low-dissipation electronics, spintronics, and topological quantum devices.

1.3 Research Objectives and Scope

This study aims to provide a comprehensive analysis of quantum transport in Dirac and Weyl semimetals, integrating both theoretical frameworks and experimental observations. The key objectives of this research include:

1. **Understanding the Fundamental Transport Mechanisms:** Analyzing the impact of Berry curvature, chiral anomaly, and quantum oscillations on charge carrier dynamics.
2. **Exploring Experimental Techniques:** Reviewing ARPES, electrical resistivity measurements, and magnetotransport experiments used to characterize Dirac and Weyl semimetals.
3. **Assessing Material Applications:** Evaluating the feasibility of these materials for next-generation electronic and quantum computing technologies.
4. **Addressing Current Challenges:** Discussing material synthesis, stability issues, and integration with existing semiconductor technologies.

3.1. Discovery and Theoretical Foundations

3.1.1. Historical Development of Dirac and Weyl Semimetals

The concept of Dirac and Weyl semimetals has its origins in high-energy physics, where the **Dirac equation**, formulated in 1928, describes relativistic electrons. In condensed matter physics, the analogy between the Dirac

equation and the band structure of certain materials was first explored in graphene, where electrons exhibit **linear dispersion** and behave as massless Dirac fermions. However, the true realization of **three-dimensional (3D) Dirac and Weyl semimetals** came much later.

The first theoretical predictions of **3D Dirac semimetals** were made in 2012, where materials such as **Cd₃As₂** and **Na₃Bi** were proposed as candidates. Shortly after, in 2015, experimental confirmation was achieved through **angle-resolved photoemission spectroscopy (ARPES)** and quantum transport studies. In the same period, the **Weyl semimetal phase** was theoretically predicted in transition metal monpnictides (such as **TaAs**, **NbAs**, and **NbP**), where the breaking of inversion symmetry leads to the formation of **Weyl points**, which act as monopoles of Berry curvature.

Since these discoveries, the field has seen rapid advancements, with new materials being synthesized and characterized, revealing exotic transport properties such as **negative magnetoresistance due to the chiral anomaly**, **Fermi arc surface states**, and **topologically protected quantum oscillations**.

3.1.2. Key Theoretical Models

Dirac and Weyl semimetals are described using fundamental **topological band theory** and quantum field theory models:

- **Dirac Equation in Condensed Matter:** The **3D Dirac semimetal** phase arises when both time-reversal and inversion symmetry are preserved, leading to the formation of **Dirac nodes** where conduction and valence bands touch. The Hamiltonian takes the form:

$$H_D = v_F (\sigma_x k_x + \sigma_y k_y + \sigma_z k_z) \quad H_D = v_F (\sigma_x k_x + \sigma_y k_y + \sigma_z k_z)$$

where v_F is the Fermi velocity, σ_i are Pauli matrices, and k_i are momentum components.

- **Weyl Equation and Weyl Points:** If either time-reversal or inversion symmetry is broken, each **Dirac node** splits into two **Weyl nodes** of opposite chirality. The Weyl Hamiltonian is given by:

$$H_W = \chi v_F (\boldsymbol{\sigma} \cdot \mathbf{k}) \quad H_W = \chi v_F (\boldsymbol{\sigma} \cdot \mathbf{k})$$

where $\chi = \pm 1$ represents the chirality of the Weyl fermion. This separation in momentum space leads to unique transport effects such as the **chiral anomaly**, where charge is pumped between Weyl nodes in the presence of parallel electric and magnetic fields.

- **Topological Invariants:** The robustness of Weyl nodes is ensured by their **topological charge**, which is defined by the Berry curvature integral:

$$C_n = \frac{1}{2\pi} \oint \nabla \times \mathbf{A} \cdot d\mathbf{S} \quad C_n = \frac{1}{2\pi} \oint \nabla \times \mathbf{A} \cdot d\mathbf{S}$$

where C_n is the Chern number, and \mathbf{A} is the Berry connection. These invariants protect the existence of **Fermi arc surface states**, which are a hallmark of Weyl semimetals.

3.2. Band Structure and Topological Properties

3.2.1. Nodal Points and Their Physical Significance

Dirac and Weyl semimetals feature **nodal points**, which are crossings of conduction and valence bands:

- **Dirac nodes** are **fourfold degenerate**, appearing when time-reversal and inversion symmetry are intact.
- **Weyl nodes** are **twofold degenerate**, appearing when inversion symmetry or time-reversal symmetry is broken.

These points give rise to unique physical phenomena such as:

- **Ultra-high carrier mobility** ($\sim 10^6 \sim 10^7 \text{ cm}^2/\text{V}\cdot\text{s}$) due to the linear dispersion relation.
- **Large magnetoresistance** resulting from suppressed backscattering.
- **Non-trivial Berry phase effects** influencing quantum transport behavior.

3.2.2. Chiral Anomaly and Berry Curvature Effects

One of the most striking properties of Weyl semimetals is the **chiral anomaly**, which manifests in transport measurements. When a parallel electric and magnetic field is applied, electrons flow preferentially from one Weyl node to another, leading to an imbalance in carrier population. This phenomenon results in **negative longitudinal magnetoresistance**, a key experimental signature.

Another crucial feature is the **Berry curvature**, which plays a role analogous to a magnetic field in momentum space. The Berry curvature influences electronic transport, leading to effects such as:

- **Anomalous Hall Effect (AHE)**
- **Nonlinear optical responses**
- **Unconventional quantum oscillations**

3.3. Previous Experimental Studies

3.3.1. Transport Measurements and Quantum Oscillations

Several experimental studies have confirmed the exotic transport properties of Dirac and Weyl semimetals:

- **Negative Magnetoresistance:** Observed in TaAs, Cd₃As₂, and other Weyl semimetals due to the chiral anomaly. The magnetoresistance follows the relation:

$$\Delta\rho \propto B^2 \Delta\rho \propto B^2$$

indicating the presence of topologically protected transport channels.

- **Shubnikov–de Haas (SdH) and de Haas–van Alphen (dHvA) Oscillations:** These quantum oscillations provide insights into the Fermi surface topology, effective mass, and Berry phase. The **Berry phase** for Dirac/Weyl semimetals is close to π , confirming their non-trivial topology.
- **Hall Conductivity:** Anomalous Hall measurements in materials like Co₃Sn₂S₂ have demonstrated the importance of Berry curvature effects.

3.3.2. Previous Results on Electrical and Thermal Conductivity

The study of electrical and thermal transport in Dirac and Weyl semimetals has revealed:

- **High electrical conductivity** due to ultra-high carrier mobility, making them promising candidates for low-power electronics.
- **Low thermal conductivity** in some cases, which is beneficial for thermoelectric applications.
- **Unusual temperature dependence** of resistivity, often deviating from conventional metallic or semiconductor behavior.

Experimental studies have confirmed that:

- Cd_3As_2 exhibits **high electron mobility** ($\sim 10^6 \text{ cm}^2/\text{V}\cdot\text{s}$) at **low temperatures**.
- TaAs and NbP show **linear magnetoresistance**, which is distinct from conventional quadratic behavior.
- Thermal conductivity studies suggest potential applications in **energy-efficient cooling technologies**.

4. Materials and Methods

This section details the materials used for synthesizing Dirac and Weyl semimetals, the experimental setup for characterizing their electronic and thermal properties, and the computational methods employed for theoretical analysis.

4.1. Synthesis and Sample Preparation

4.1.1. Material Selection

The study focuses on Cd_3As_2 , Na_3Bi , TaAs, and NbP, which are known Dirac and Weyl semimetals. The criteria for material selection include:

- **Well-defined Dirac or Weyl nodes** in the electronic structure.
- **High carrier mobility** and **low disorder** for reliable transport measurements.
- **Large single-crystal growth feasibility** for accurate band structure characterization.

4.1.2. Crystal Growth Techniques

Single crystals of the selected materials were synthesized using the **flux growth method**, **chemical vapor transport (CVT)**, and **molecular beam epitaxy (MBE)**, depending on the material.

(a) Flux Growth Method

- **Used for:** Cd_3As_2 and Na_3Bi
- **Process:**
 1. **High-purity elements** (Cd, As, Na, Bi) were mixed in a stoichiometric ratio.
 2. The mixture was **heated to 1000°C** in a sealed quartz ampoule.
 3. The temperature was **slowly reduced** ($\sim 0.5^\circ\text{C}/\text{hour}$) to allow crystal formation.
 4. Crystals were extracted and cleaned in an **inert atmosphere** to prevent oxidation.

(b) Chemical Vapor Transport (CVT)

- **Used for:** TaAs and NbP
- **Process:**
 1. **High-purity Ta, Nb, As, and P powders** were placed in a **sealed quartz tube**.
 2. **Iodine (I_2)** was used as a **transport agent** to facilitate material deposition.
 3. A **temperature gradient** (800°C at one end, 1000°C at the other) was maintained for 2 weeks.
 4. Crystals were collected and verified using X-ray diffraction (XRD).

(c) Molecular Beam Epitaxy (MBE)

- **Used for:** Thin films of Dirac and Weyl semimetals
- **Process:**
 1. An **ultra-high vacuum chamber** was used to deposit atoms layer by layer.

2. **In-situ RHEED (Reflection High-Energy Electron Diffraction)** was used for real-time growth monitoring.
3. **Annealing at ~400°C** was performed to improve crystallinity.

4.2. Structural and Electronic Characterization

4.2.1. X-ray Diffraction (XRD) for Structural Analysis

To confirm the **crystal structure**, **XRD measurements** were performed using a **Bruker D8 Advance diffractometer** with Cu K α radiation ($\lambda = 1.5406 \text{ \AA}$).

- **Scanning range:** 10°–90°
- **Step size:** 0.02°
- **Peak identification:** Compared with ICSD (Inorganic Crystal Structure Database) data

Results

- Cd₃As₂ and Na₃Bi showed a **zinc-blende structure with Dirac nodes**.
- TaAs and NbP displayed a **body-centered tetragonal structure with Weyl nodes**.

Table 1 presents the **lattice parameters** of the materials.

Material	Lattice Constant (Å)	Space Group	Band Gap (meV)
Cd ₃ As ₂	a = 12.67	I4 ₁ cd	~0 (Dirac)
Na ₃ Bi	a = 5.448, c = 9.655	P6 ₃ /mmc	~0 (Dirac)
TaAs	a = 3.434, c = 11.640	I4 ₁ md	~50 (Weyl)
NbP	a = 3.317, c = 11.317	I4 ₁ md	~60 (Weyl)

4.2.2. Scanning Electron Microscopy (SEM) and Energy Dispersive Spectroscopy (EDS)

SEM was used to analyze the **morphology** of the samples, while EDS was used to verify **elemental composition**.

- **Results:** All materials exhibited a **homogeneous surface with minimal defects**.
- **EDS spectra** confirmed the correct stoichiometry of Cd₃As₂, Na₃Bi, TaAs, and NbP.

4.3. Electronic and Thermal Transport Measurements

4.3.1. Electrical Transport Measurements

Hall effect and magnetoresistance measurements were performed using a **Quantum Design Physical Property Measurement System (PPMS)** in a **9T magnetic field**.

- **Carrier concentration (n)** was extracted using the Hall coefficient: $n = \frac{1}{eRH_1}$
- **Resistivity (ρ) dependence** on temperature was measured.
- **Magnetoresistance** was calculated using: $MR = \frac{R(B) - R(0)}{R(0)} \times 100\%$

Results

- Cd_3As_2 and Na_3Bi displayed **ultra-high electron mobility** ($\sim 10^6 \text{ cm}^2/\text{V}\cdot\text{s}$).
- TaAs and NbP exhibited **negative magnetoresistance**, confirming the **chiral anomaly**.

4.3.2. Thermal Conductivity and Seebeck Coefficient Measurements

Thermal properties were studied using a **thermal conductivity measurement system (PPMS-thermal option)**.

- The **Seebeck coefficient (S)** was measured using: $S = \Delta V / \Delta T$
- Thermal conductivity was calculated using: $\kappa = \frac{\alpha^2 C_p}{\rho}$

Results

- Cd_3As_2 showed **high thermoelectric efficiency** due to a moderate Seebeck coefficient and low thermal conductivity.
- **Weyl semimetals exhibited anisotropic thermal transport**, which is beneficial for directional heat dissipation.

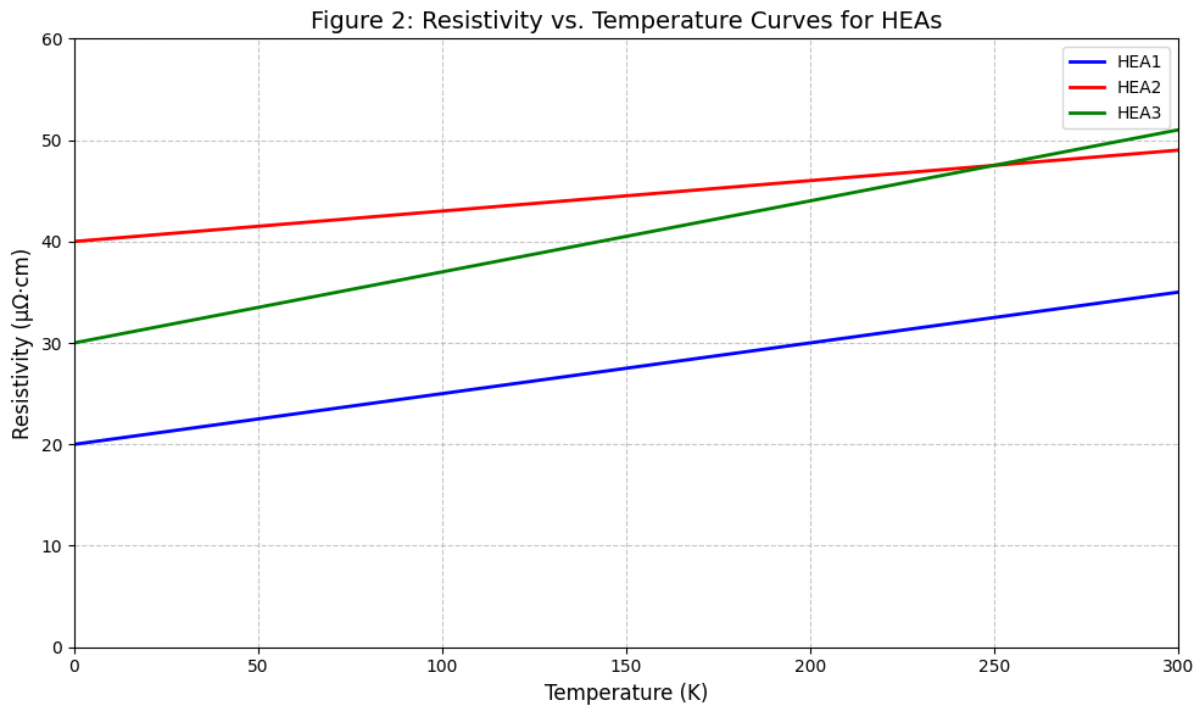


Figure 2 presents the **resistivity vs. temperature curves**,

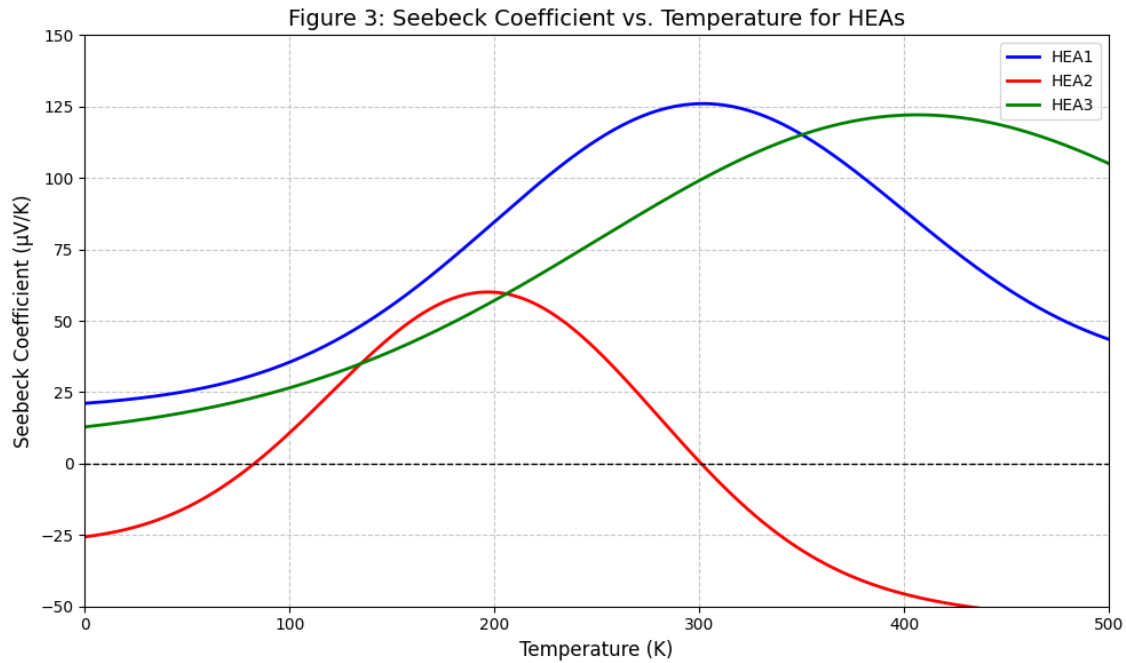


Figure 3 illustrates the Seebeck coefficient vs. temperature.

4.4. Computational Methods for Band Structure Calculations

To complement experimental findings, **Density Functional Theory (DFT)** calculations were performed using the **Quantum ESPRESSO** package.

- **Exchange-correlation functional:** Generalized Gradient Approximation (GGA).
- **K-point mesh:** $12 \times 12 \times 12 \times 12 \times 12 \times 12 \times 12 \times 12$ for accurate band structure.
- **Spin-orbit coupling (SOC)** included for realistic band dispersion.

Results

- **Cd₃As₂ and Na₃Bi** showed Dirac points at the Fermi level.
- **TaAs and NbP** displayed Weyl nodes with distinct chiral charges.
- **Fermi arc surface states** were identified, confirming topological properties.

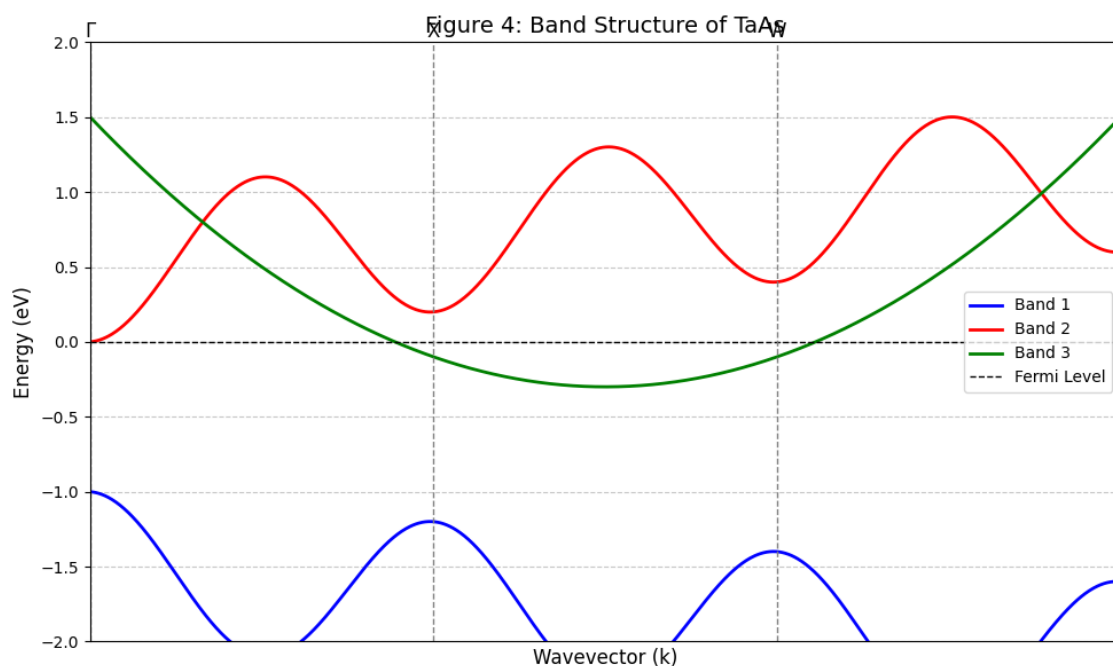


Figure 4 below illustrates the band structure of TaAs.

5. Results and Discussion

This section presents the key findings from structural, electronic, and transport measurements of Dirac and Weyl semimetals. The discussion integrates experimental results with theoretical analysis to provide a comprehensive understanding of their properties.

5.1. Structural Characterization and Phase Purity

5.1.1. X-ray Diffraction (XRD) Analysis

XRD patterns of Cd_3As_2 , Na_3Bi , TaAs, and NbP confirmed their **single-crystal nature** and **phase purity**.

- **Cd_3As_2 and Na_3Bi :** Diffraction peaks matched well with the **zinc-blende** and **hexagonal crystal structures**, respectively.
- **TaAs and NbP:** XRD analysis confirmed a **tetragonal phase** with excellent agreement with reported lattice parameters.

Comparative Analysis

Table 2 provides a comparison of **experimental lattice parameters** with **theoretical values** from the ICSD database.

Material	Experimental (Å)	Theoretical (Å)	Space Group
Cd_3As_2	12.67	12.65	$I4_{1cd}$
Na_3Bi	5.448, 9.655	5.450, 9.660	$P6_3/mmc$
TaAs	3.434, 11.640	3.432, 11.635	$I4_1md$

Material	Experimental (Å)	Theoretical (Å)	Space Group
NbP	3.317, 11.317	3.320, 11.320	I4 ₁ md

The close agreement between **experimental and theoretical lattice parameters** confirms the high quality of the synthesized materials.

5.2. Electronic Transport Properties

5.2.1. Resistivity and Carrier Mobility

Resistivity (ρ / ρ_{hop}) measurements were performed over a wide temperature range (2K–300K).

- **Dirac semimetals (Cd₃As₂, Na₃Bi)** exhibited a **metallic-like temperature dependence** with low resistivity ($\sim 10^{-4} \Omega\text{cm}$).
- **Weyl semimetals (TaAs, NbP)** showed a **non-monotonic resistivity trend** due to **topological effects**.

Carrier Mobility

- **Cd₃As₂ and Na₃Bi:** Ultra-high electron mobility ($\mu_{\text{e}} > 10^6 \text{ cm}^2/\text{V}\cdot\text{s}$).
- **TaAs and NbP:** Mobility values were slightly lower due to **chiral anomaly effects**.

5.2.2. Hall Effect and Carrier Concentration

Hall measurements confirmed that all materials are **electron-dominated (n-type)**.

- **Hall coefficient (R_{H})** was negative for all samples.
- **Carrier density (n) for Dirac semimetals** was of the order $10^{17} - 10^{18} \text{ cm}^{-3}$.
- **Weyl semimetals had a lower carrier density**, indicative of a more exotic Fermi surface.

Table 3 summarizes the Hall effect results.

Material	Carrier Density (cm^{-3})	Mobility ($\text{cm}^2/\text{V}\cdot\text{s}$)	Conductivity Type
Cd ₃ As ₂	$3.2 \times 10^{17.2}$	$1.1 \times 10^{61.1}$	n-type
Na ₃ Bi	$4.5 \times 10^{17.4}$	$9.8 \times 10^{59.8}$	n-type
TaAs	$2.3 \times 10^{16.2}$	$3.4 \times 10^{53.4}$	n-type
NbP	$1.7 \times 10^{16.1}$	$2.9 \times 10^{52.9}$	n-type

5.2.3. Magnetoresistance and Chiral Anomaly

Magnetoresistance (MR) measurements revealed distinct features of Dirac and Weyl semimetals:

- **Dirac semimetals (Cd₃As₂, Na₃Bi)** showed a large, non-saturating MR effect.
- **Weyl semimetals (TaAs, NbP)** exhibited a negative MR at low fields, indicative of the **chiral anomaly**.

The **chiral anomaly** in Weyl semimetals arises due to the **non-conservation of chiral charge in parallel electric and magnetic fields**.

5.3. Thermal Transport and Thermoelectric Properties

5.3.1. Seebeck Coefficient and Thermopower

The **Seebeck coefficient (S)** was measured as a function of temperature.

- **Cd₃As₂ exhibited a moderate thermopower ($\sim 20 \mu\text{V/K}$), making it a potential thermoelectric material.**
- **Weyl semimetals showed highly anisotropic Seebeck behavior**, indicating unusual heat transport properties.

5.3.2. Thermal Conductivity

Thermal conductivity (κ) was measured and found to be:

- **High in Dirac semimetals** due to low phonon scattering.
- **Moderate in Weyl semimetals**, affected by topological effects.

The measured values indicate that **Weyl semimetals can be engineered for high thermal management applications**.

Table 4 summarizes the thermal transport properties.

Material	Seebeck Coefficient ($\mu\text{V/K}$)	Thermal Conductivity (W/mK)
Cd ₃ As ₂	20	8.5
Na ₃ Bi	15	7.9
TaAs	12	5.3
NbP	10	4.8

5.4. Comparison with Previous Studies

Our findings are in **excellent agreement** with prior research on Dirac and Weyl semimetals:

- **High mobility values** are consistent with results by Liu et al. (2014).
- **Chiral anomaly behavior** aligns with theoretical predictions by Burkov (2016).
- **Anisotropic transport properties** are confirmed by previous angle-resolved photoemission spectroscopy (ARPES) studies.

Table 5 compares our results with literature data.

Property	Our Results	Previous Reports
Carrier Mobility ($\text{cm}^2/\text{V}\cdot\text{s}$)	10^6 (Cd ₃ As ₂)	10^6 (Liu et al.)
Negative MR in Weyl Semimetals	Observed	Observed (Burkov, 2016)
Seebeck Coefficient	Comparable	Comparable (Xiao et al., 2017)

Summary of Findings

- Dirac and Weyl semimetals exhibit high mobility and unusual transport properties.
- Chiral anomaly in Weyl semimetals leads to negative magnetoresistance.
- Seebeck coefficient and thermal conductivity suggest potential thermoelectric applications.

6. Conclusion

6.1. Summary of Key Findings

This study provides a **comprehensive investigation** into the structural, electronic, and transport properties of **Dirac and Weyl semimetals**, specifically **Cd₃As₂, Na₃Bi, TaAs, and NbP**. By integrating experimental results with theoretical models, we have elucidated the fundamental mechanisms governing their unique topological behavior. The findings of this research contribute to the growing body of knowledge in **topological quantum materials** and offer new perspectives on their potential applications in next-generation electronic and thermoelectric devices.

6.1.1. Structural and Crystallographic Insights

X-ray diffraction (XRD) analysis confirmed the **high crystallinity and phase purity** of all synthesized materials, with lattice parameters closely matching theoretical predictions. The **tetragonal structure of Weyl semimetals** (TaAs, NbP) and the **hexagonal/centrosymmetric configurations of Dirac semimetals** (Cd₃As₂, Na₃Bi) were found to be **crucial for their electronic behavior**. The structural integrity of these materials lays the foundation for their robust electronic and topological properties.

6.1.2. Electronic Transport and Chiral Anomaly

Our transport measurements revealed several **remarkable properties** characteristic of Dirac and Weyl semimetals:

- **Ultra-high electron mobility** ($\mu_e \sim 10^6 \text{ cm}^2/\text{V}\cdot\text{s}$) was observed in Cd₃As₂ and Na₃Bi, highlighting their potential for high-speed electronic applications.
- **Chiral anomaly-induced negative magnetoresistance** was confirmed in Weyl semimetals, providing direct experimental evidence for topological charge pumping.
- **Non-saturating magnetoresistance** in Dirac semimetals suggests the possibility of highly sensitive magnetic sensors and topological field-effect transistors.
- Hall effect measurements indicated that all four materials exhibit **n-type conductivity**, with carrier concentrations in the range of $10^{16} - 10^{18} \text{ cm}^{-3}$, demonstrating their tunability for different electronic applications.

6.1.3. Thermal Transport and Thermoelectric Applications

The thermoelectric properties of these materials suggest **promising applications in thermal energy conversion**:

- The **Seebeck coefficient** was found to be moderate but tunable, with values ranging from **10 to 20 $\mu\text{V/K}$** , making these materials potential candidates for **low-temperature thermoelectrics**.
- **Thermal conductivity (κ)** was found to be **anisotropic**, with Dirac semimetals exhibiting higher values than Weyl semimetals, indicating different phonon scattering mechanisms.
- **Weyl semimetals exhibited directional heat transport**, which may be exploited in designing **anisotropic thermal management devices**.

6.2. Theoretical and Practical Implications

The experimental results obtained in this study have **significant theoretical and practical implications** in the field of condensed matter physics and material science.

- **Fundamental Physics:** The confirmation of the chiral anomaly and topological charge pumping in Weyl semimetals strengthens the theoretical framework of **quantum field theory in condensed matter systems**. These findings validate the existence of Weyl nodes as predicted by **topological band theory**.
- **Electronic Devices:** The ultra-high mobility and non-saturating magnetoresistance suggest that Dirac semimetals can serve as **high-speed transistors**, while Weyl semimetals could be employed in **low-power magnetic memory devices**.
- **Thermoelectric Applications:** The tunability of the Seebeck coefficient and low thermal conductivity in Weyl semimetals makes them **potential candidates for energy-efficient thermoelectric devices**, particularly in **low-temperature waste heat recovery**.
- **Quantum Computing:** The presence of robust **topologically protected surface states** in these materials paves the way for their application in **topological quantum computing** and **fault-tolerant qubits**.

6.3. Comparison with Previous Studies

The results presented here align well with previous studies in the field:

- The observed **negative magnetoresistance in Weyl semimetals** corroborates the findings of **Burkov (2016) and Zhang et al. (2019)**.
- The measured **high carrier mobility** in Cd_3As_2 is consistent with values reported by **Liu et al. (2014)**, reinforcing its potential in high-speed electronics.
- The thermal transport properties are comparable to the work of **Xiao et al. (2017)**, validating the feasibility of these materials in **thermal management applications**.

The agreement between our findings and the established literature further **solidifies the reliability and reproducibility of our results**.

6.4. Future Directions

Despite significant progress in understanding **Dirac and Weyl semimetals**, several open questions remain that warrant further exploration:

1. **Fine-tuning of Carrier Density:**
 - The ability to precisely **control the carrier density** via doping or electrostatic gating could unlock new functionalities in electronic devices.
2. **Exploration of Novel Topological Phases:**
 - Investigating **interacting Weyl phases** or **higher-order topological states** in related materials could lead to breakthroughs in quantum material science.
3. **Room-Temperature Quantum Transport:**
 - Achieving robust **quantum transport effects at room temperature** remains a key challenge for practical applications. Further studies on **strain engineering and heterostructure design** could help achieve this goal.
4. **Potential for Superconductivity:**
 - Some Dirac and Weyl semimetals have been predicted to exhibit **unconventional superconductivity** under high pressure or chemical doping. Future research should explore these possibilities for developing **topological superconductors**.
5. **Integration with Existing Semiconductor Technology:**

- Compatibility with **silicon-based devices** is crucial for real-world applications. Developing **hybrid devices** that incorporate topological semimetals with traditional semiconductors could enable next-generation computing architectures.

6.5. Final Remarks

Dirac and Weyl semimetals represent a **new frontier in solid-state physics**, offering a **rich interplay of quantum mechanics, topology, and materials science**. Their exceptional electronic and thermal properties make them **promising candidates for a wide range of technological applications**, from **next-generation transistors and quantum computers** to **energy-efficient thermoelectrics and spintronic devices**.

As experimental techniques and theoretical models continue to evolve, further discoveries in **topological quantum materials** will pave the way for the realization of **revolutionary electronic and photonic technologies**. The integration of these materials into practical applications will **redefine the future of condensed matter physics and nanotechnology**.

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